

1 - 02/7/16

STACKS

UNIT - II

- Stack is a linear data structure which is based on LIFO (Last in First out).
- With stacks insertions and deletions happens through only one end called top of the stack.
- Inserting into the stack is called push operation.
- Deleting from the stack is called pop operation.
- If there is no space in the stack to insert a new element then it is called stack overflow.
- When the stack is empty, and we try doing any operations, then it is stack underflow.
- We can implement the stack concept in 2 ways.
 - (i) arrays
 - (ii) linked list.

Applications of Stack:

- Converting an infix expression to its postfix notation.
- Evaluating the postfix expression.
- Nested function calls.
- Recursion.

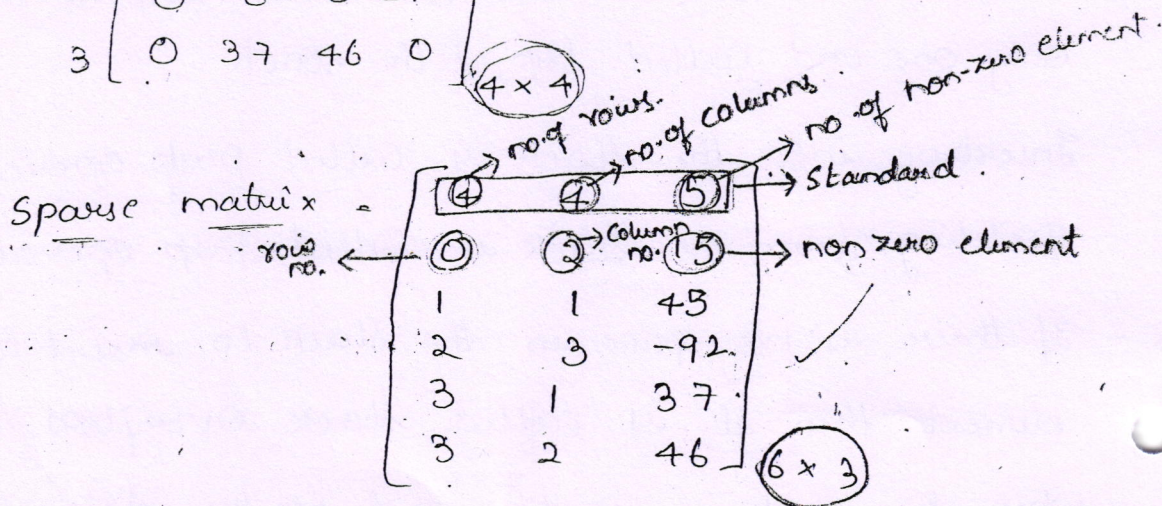
St:
{
in
in
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r
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{
if
e
Voi
{
if
Pf
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y

Sparse Matrix Representation :-

Array Representation

eg:-

		0	1	2	3
0	0	0	15	0	
1	0	45	0	0	
2	0	0	0	-92	
3	0	37	46	0	



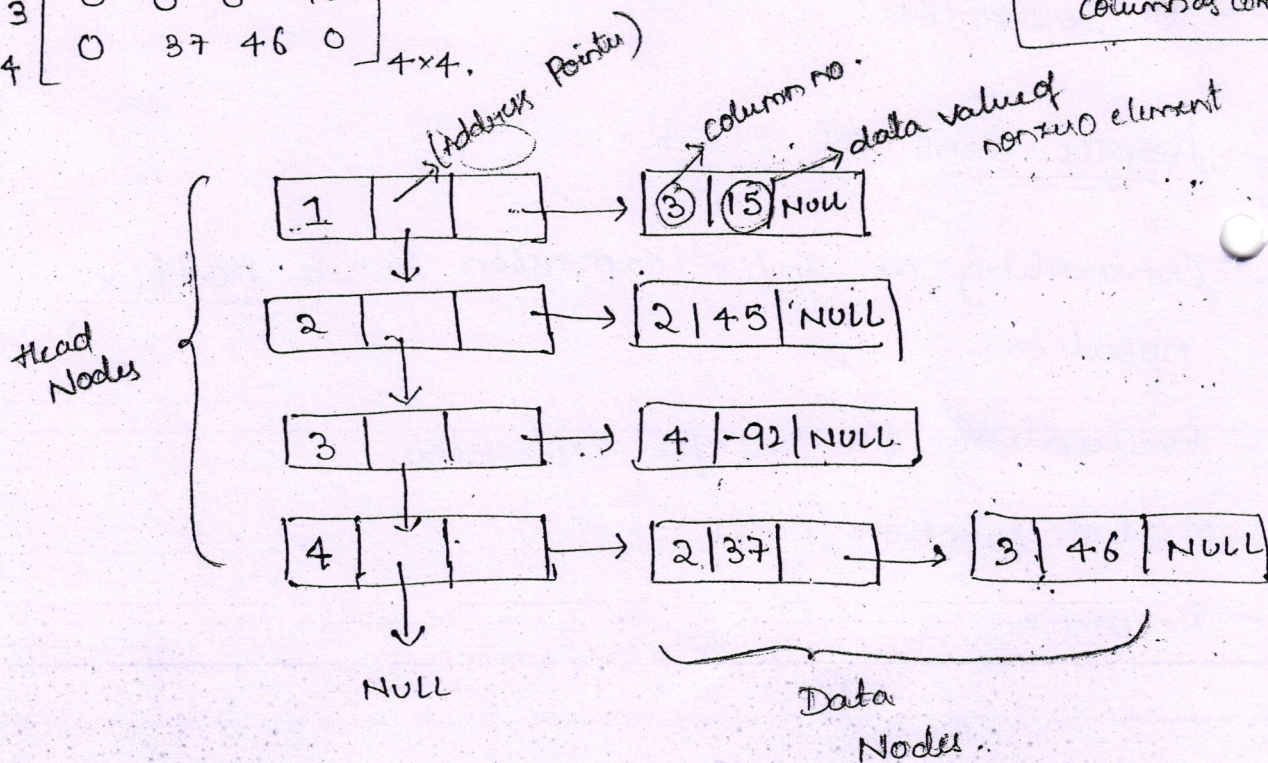
Linked Representation :-

[row is taken as column]

	1	2	3	4
1	0	0	15	0
2	0	45	0	0
3	0	0	0	-92
4	0	37	46	0

4x4.

⇒ Same linked representation can also be done by taking columns as common



define Size 10

struct stack.

```
{  
  int S[SIZE];  
  int top;  
} st;
```

int isst overflow()

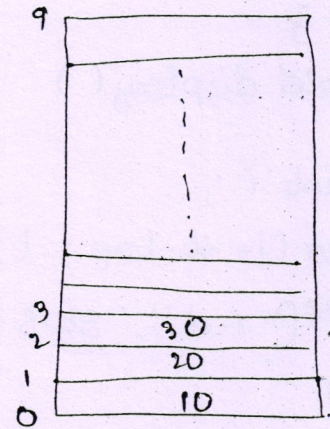
```
{  
  int x;  
  if (st.top >= SIZE-1)  
    x = 1;  
  else  
    x = 0;  
  return x;  
}
```

int isst underflow()

```
{  
  int x;  
  if (st.top == -1)  
    x = 1;  
  else  
    x = 0;  
  return x;  
}
```

void push (int x)

```
{  
  if (isst overflow() == 1)  
    Pf ("Stack overflow = 1.d", x);  
  else {  
    st.top++;  
    st.S[st.top] = x;  
    Pf ("inserted");  
  }  
}
```



```

void pop ()
{
    int x;
    if (isstackunderflow() == 1)
        Pf("Stack underflow")
    else
    {
        x = st.s[st.top];
        st.top--;
        Pf("Element to be delete = %d", x);
    }
}

```

```

void display ()
{
    int i;
    for (i = st.top; i >= 0; i--)
        Pf("%d", st.s[i])
}

```

```

void main ()
{
    st.top = -1;
    push(10);
    push(20);
    push(30);
    display();
    pop();
    display();
}

```

```

void main () {
    st.top = -1;
    int x;
    char ch;
    do {
        Pf("enter the elements");
        Sf("%d", &x);
        push(x);
        Pf("do you wish to continue (y/n)");
        getch();
        ch = getch();
    } while (ch != 'y');
    display();
    pop();
    display();
}

```

4/7
 St
 St
 St
 y
 void
 int
 do {
 Pf (" %d",
 Sf (" %d",
 newn
 new
 new
 if (
 else
 Pf
 ge
 ch
 y
 wh
 }

4/7/16

Stack Using Linked List :-

```
# include <stdio.h>
# include <stdlib.h>
```

```
struct node {
    int data;
    struct node * link;
} * top = NULL;
```

```
void push () {
```

```
    struct node * newnode;
    int x, char choice;
    do {
```

```
        printf ("Enter the numbers ");
        scanf ("%d", &x);
```

```
        newnode = (struct node *) malloc (sizeof (struct node));
```

```
        newnode -> data = x;
        newnode -> link = NULL;
```

```
        if (top == NULL)
            {
                top = newnode;
            }
        }
    else
```

```
        {
            newnode -> link = top;
            top = newnode;
        }
    }
```

```
    printf ("do you wish to continue (y/n)");
```

```
    get char ();
    choice = get char ();
```

```
    }
    while (choice == 'y');
```

```
    }
```

```
void display ( )
```

```
{
```

```
struct node *temp = top;
```

```
while (temp != NULL)
```

```
{
```

```
  printf("%d", temp->data);
```

```
  temp = temp->link;
```

```
}
```

```
}
```

```
void pop ( ) {
```

```
  struct node *temp = top;
```

```
  if (top == NULL)
```

```
  {
```

```
    printf("cannot delete")
```

```
  }
```

```
  else {
```

```
    top = top->link;
```

```
  }
```

```
}
```

```
void main ( ) {
```

```
  push ( );
```

```
  display ( );
```

```
  pop ( );
```

```
  display ( );
```

```
}
```

5/7/16

C

1) Rec

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3) Sto

info

4) If

5) " :"

exp

6) If

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w:

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- Noc

7) If

Rem

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8) Ret

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9) D.

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Level of Priority

#

^

*, /, %

+, -

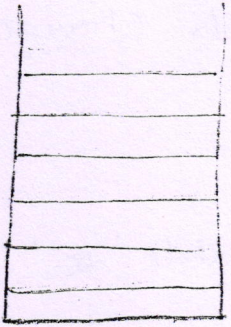
C.

5/7/16

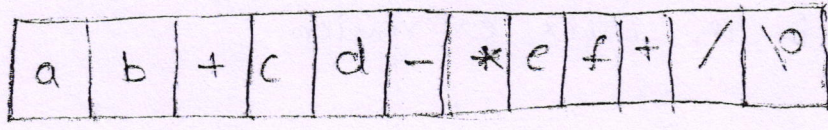
Converting Infix Expression to its Postfix form.

- 1) Read the infix expression.
- 2) Repeat steps 3, 4, 5, 6, 7, 8 for the each character in the infix expression.
- 3) Store current character in the variable 'x' infix expression in the variable 'x'.
- 4) If 'x' is left bracket (() Put it in the stack.
- 5) If 'x' is an operand write it on the postfix expression.
- 6) If 'x' is right bracket () for each operators then remove all the operators ^{from} ~~for~~ the stack and write them on the postfix expression until, we get the left bracket in the stack,
- Now remove left bracket the stack.
- 7) If 'x' is an operator
Remove all the operators ^{from} ~~for~~ the stack whose precedence is greater than or equal to 'x'.
Then, put them _{into postfix} and then put the operator 'x' in the stack.
- 8) Retrieve next character into 'x' until you reach NULL character.
- 9) Display the characters stored in postfix expression.

Infix Expression: $((a+b) * (c-d) / (e+f))$



Stack



Postfix Expression

```
#
#
char St[20];
int top = -1;
void Push (char x)
{
    top ++;
    St[top] = x;
}
char Pop()
{
    char x;
    x = St[top];
    top --;
    return x;
}
```

```
int
{
if (
else
}
int p
{
if (
else if
else if
else
}
void
{
char
char
int
pf()
gets()
for
{
x
if
}
```



```
int isoperator (int Char x)
```

```
{  
if (x == '+' || x == '-' || x == '*' || x == '/')
```

```
return 1;
```

```
else
```

```
return 0;
```

```
}  
int prec (Char x)
```

```
{  
if (x == '^')
```

```
return 4;
```

```
else if (x == '*' || x == '/' || x == '%')
```

```
return 3;
```

```
else if (x == '+' || x == '-')
```

```
return 2;
```

```
else
```

```
return 1;
```

```
}
```

```
void main ()
```

```
{  
char infix [80], postfix [80];
```

```
char x, y;
```

```
int i, j = 0;
```

```
printf ("enter infix expression");
```

```
gets (infix);
```

```
for (i = 0 ; infix [i] != '\0' ; i++)
```

```
{  
x = infix [i];
```

```
if (x == 'C')
```

```
{  
push (x);
```

```
}
```

^	4
*, /, %	3
+, -	2
(,)	1

else if (x == '(')

{
while (st[top] != '(')

{
postfix[j] = pop();

j++;

}

~~pop();~~

pop();

}

else if (isoperator(x))

{
while (prec(st[top]) >= prec(x))

{
postfix[j] = pop();

j++;

}

push(x);

}

else if (x >= 'a' && x <= 'z')

{
postfix[j] = x;

j++;

}

{

postfix[j] = '\0';

puts(postfix);

}

Post

b

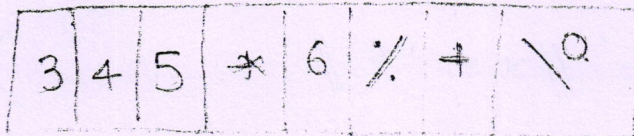
e

7

5

Postfix Evaluation

Postfix:

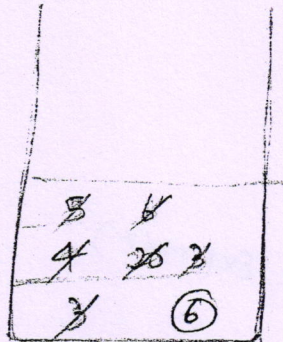


$$\left. \begin{array}{l} b=5 \\ a=4 \end{array} \right\} \textcircled{1}$$

$$b * a = 20$$

$$\left. \begin{array}{l} b=20 \\ a=6 \end{array} \right\} \textcircled{2}$$

$$20 / 6 = 3 \dots$$



$$\left. \begin{array}{l} b=3 \\ a=3 \end{array} \right\} \textcircled{3}$$

$$3 + 3 = 6$$

Ex 2: -

3	4	+	5	9	-	*	3	2	+	/
---	---	---	---	---	---	---	---	---	---	---

→ postfix.

a=97 A=65
b=98 B=:
c=:

```
#include <stdio.h>
```

```
int  
char st [20];
```

```
int top = -1;
```

```
void push (int x)
```

```
{
```

```
  top ++;
```

```
  st [top] = x;
```

```
int  
char y
```

```
pop () {
```

```
  int x;
```

```
  x = st [top];
```

```
  top --;
```

```
  return x;
```

```
}
```

'0' - 48

'1' - 49

'2' - 50

'3' - 51

```
int isoperator (char x)
```

```
{  
if (x == '+' || x == '-' || x == '*' || x == '/' || x == '^')
```

```
return 1;
```

```
else
```

```
return 0;
```

```
}
```

```
void main ( )  
= PF ("Enter the Expression")  
= gets ( postfix )
```

```
{  
char postfix[80]; int i; char x; int a, b;
```

```
for (i=0; postfix[i] != '\0'; i++)
```

```
{  
x = postfix[i];
```

```
if (x >= '0' && x <= '9')
```

```
push (x - 48);
```

```
else if (isoperator(x))
```

```
{  
b = POP();
```

```
a = POP();
```

```
switch (x)
```

```
{  
case '+': push (a+b); break;
```

```
case '*': push (a*b); break;
```

```
...
```

```
}
```

```
}
```

```
PF ("%d", st[top]);
```

```
}
```

11/7/11

- Qu

for

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(i)

(ii)

Impl

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- FCI

- use

* In

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11/7/16

Queue

- Queue is a linear data structure which follows first in first out (FIFO) mechanism, follows linear mechanism.
- Inserting data into the queue is called Enqueuing / enqueue operation.
- Deleting data from the queue is called dequeuing / dequeue operation.
- Queue Overflow :- when there is no space in the queue to add a new element is known as queue overflow.
- Queue Underflow :- when there are no elements in the queue to remove elements is known as queue underflow.
- The mechanism queue is implemented in 2 ways.
 - (i) Arrays.
 - (ii) linked-list.

Applications of Queue :-

- FCFS C.P.U scheduling algorithm.
(first come first serve)
- usage of a Printer in a shared networking environment.
- * Insertions into the queue we do through rear.
- * Deletions through front.

Queue Using arrays

```
# define SIZE 10
```

```
int f = -1, r = -1;
```

```
int Q [SIZE];
```

```
int is q full()
```

```
{
```

```
if (r >= SIZE - 1)
```

```
return 1;
```

```
else
```

```
return 0;
```

```
}
```

```
int is q empty()
```

```
{
```

```
if (f == -1)
```

```
return 1;
```

```
else
```

```
return 0;
```

```
}
```

```
void enqueue (int x)
```

```
{ if (is q full() == 1)
```

```
    Pf ("Queue overflow");
```

```
else {
```

```
    r++;
```

```
    Q[r] = x;
```

```
    if (f == -1)
```

```
        f = 0;
```

```
}
```

```
}
```

~~void~~

void

{

int

if (

Pf

else

for

}

?

~~void~~

{

if

else

}

}

}

```
void display()
```

```
{
```

```
    int i;
```

```
    if (is q empty() == 1)
```

```
        Pf ("NO elements to display");
```

```
    else {
```

```
        for (i = f; i <= r; i++)
```

```
            Pf ("%d ", Q[i]);
```

```
    }
```

```
}
```

```
void dequeue()
```

```
{
```

```
    if (is q empty() == 1)
```

```
        Pf ("NO elements to delete");
```

```
    else {
```

```
        x = Q[f];
```

```
        f++;
```

```
        Pf ("The element deleted = %d", x);
```

```
    }
```

```
}
```

12/7/16

Queue → Linked List

Vol

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Wti

```
#include <stdio.h>
```

```
struct node
```

```
{  
    int data;
```

```
    struct node *link;
```

```
} * f = NULL, * r = NULL;
```

```
void enqueue(  
    → insert  
)
```

```
{  
    struct node * newnode;
```

```
    int x;
```

```
    do
```

```
    {
```

```
        printf("Enter the number");
```

```
        scanf("%d", &x);
```

```
        newnode = (struct node *) malloc (size of (struct node));
```

```
        newnode → data = x;
```

```
        newnode → link = NULL;
```

```
        if (f == NULL)
```

```
        {
```

```
            f = newnode;
```

```
            [r = newnode;] (not necessary)
```

```
        }
```

```
    else
```

```
    {
```

```
        r → link = newnode;
```

```
    }
```

```
    r = newnode;
```

```
}
```



```

{
    pf ("cant insert new element");
}
else if (f == -1)
{
    f = r = 0;
    DQ[f] = x;
}
else {
    f--;
    DQ[f] = x;
}
}

```

(or)
elements can be inserted
by shifting element.

```

R++;
for (i=R; i>0; i--);
DQ[i] = DQ[i-1];
DQ[0] = x

```

```

void delete v ( )
{
    if (f == -1)
        pf ("no elements in queue to delete");
    else if (f == 0)
    {
        f = -1;
        r = -1;
    }
    else {
        r--;
    }
}

```

```

# i
# i
str
int
struct
}
var
{
str
in
do
pf
st
neu
re
re

```

a)

```

{
  f = r = 0;

```

from

```

}
else {
  r++;

```

```

}
  DS[r] = x;

```

ation

```

}
```

reted

```

}
```

be

```

void delet f ( )

```

```

{ int x;

```

```

  if (f == -1)

```

```

    pf ("empty can't delete");

```

```

  else

```

```

    { x = DS[f];

```

```

      if (f == r r)

```

```

        {

```

```

          f = -1;

```

```

          r = -1;

```

```

        }

```

```

      else

```

```

        {

```

```

          f++;

```

```

        }

```

```

        pf ("The element deleted = %d", x);

```

```

      }

```

```

    }

```

```

void insert f ( )

```

```

{

```

```

  if (f == 0)

```

tion only

d. only

e from

(Arrays) Deque (Double ended Queue)

- Dequeue stands for double ended queue.
- In Dequeue insertion and deletions can be done from both the ends i.e., front end and rear end.

They are 2 types of Dequeue.

① I/P restricted Dequeue :- where there is restriction only in insertion, i.e., elements must be inserted only from rear end and deletions can be done from both the ends.

② O/P restricted Dequeue :- where there is restriction only in deletion i.e., elements must be deleted only from front end and insertions can be done from both the ends.

```
#include <stdio.h>
```

```
#define SIZE 50
```

```
int DQ [SIZE];
```

```
int f = -1, r = -1;
```

```
void insertr(int x)
```

```
{
```

```
    if (r == SIZE - 1)
```

```
        printf ("Queue Overflow");
```

```
    else {
```

```
        if (f == -1)
```

```
}  
Void  
{ in  
  if  
  f  
else  
{  
  
else  
  
P  
}  
}  
Void  
{  
  if
```

known
all
always
used by
we read
↓

void dequeue()

```
{
    int temp;
    if (f == -1)
        pf("Queue empty");
    else
        {
            temp = cq[f];
            if (f == r)
                {
                    f = r = -1;
                }
            else
                {
                    f = (f+1) % SIZE;
                }
            pf("Element deleted = %d", temp);
        }
}
```

void display()

```
{
    int i;
    if (f == -1)
        pf("Queue empty");
    else
        {
            for (i = f; i != r; i = (i+1) % 5)
                {
                    pf("%d", cq[i]);
                }
            pf("%d", cq[r]);
        }
}
```