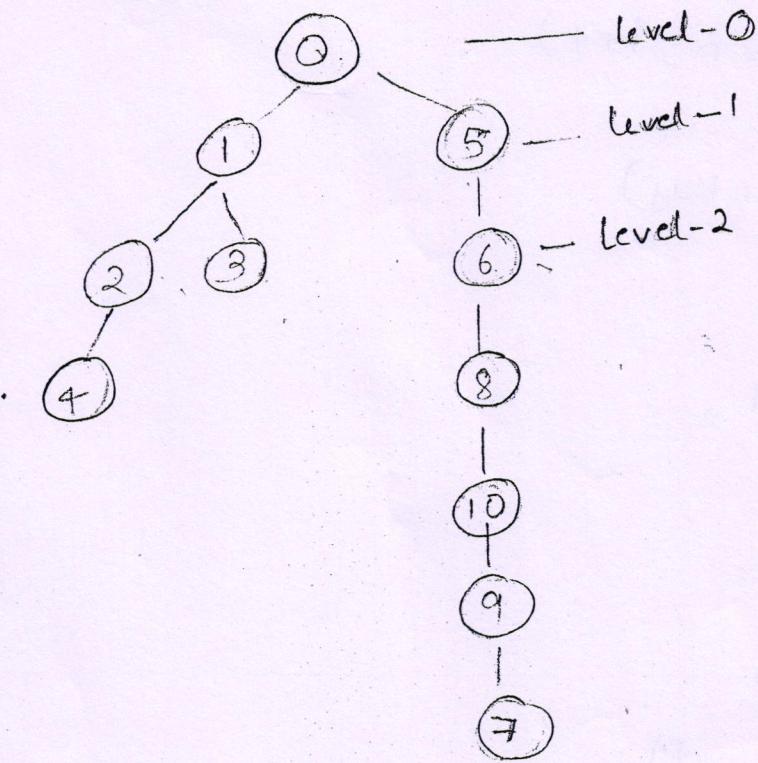


11 Vertices

Edge

- 0-1
- 0-5
- 1-2
- 7-3
- 1-5
- 2-4
- 4-3
- 5-6
- 6-8
- 7-3
- 7-8
- 8-10
- 9-7
- 10-9



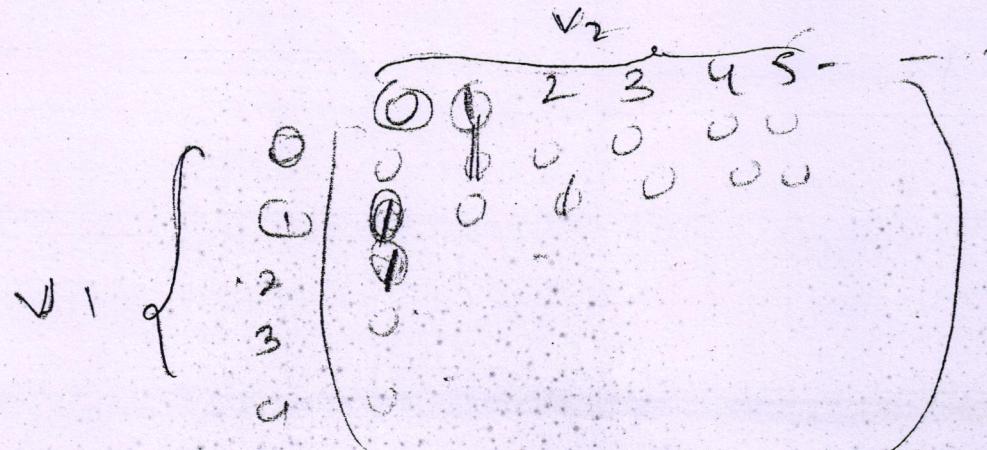
BFS ↗

DFS. - ↘

all the

DF'S :- 0, 1, 2, 4, 3, 5, 6, 8, 10, 9, 7

BF'S :- 0, 1, 5, 2, 3, 6, 4, 8, 10, 9, 7



20/8/16

UNIT 4

Searching & Sorting

Binary

[In +
ane]

Linear search

```
#include <stdio.h>
void main() {
    flag=0, pos',
    for(i=0; i<n; i++)
    {
        if (A[i] == key)
        {
            flag = 1
            pos = i+1,
            break;
        }
    }
    if (flag == 0)
        pf("not found");
    else
        pf("found at = %d", pos);
}
```

whi

or

Value

#incl
void
flag=c

low=c

Search

if

else

else, i

else

if (if

else

3

Binary Search

low 1 2 3 4 5 6 7 high

[In this we consider lower bound and high bound and then calculate the mid value, and check whether the key is towards left array or right array and then change the mid value accordingly].

```
#include <stdio.h>
```

```
void main()
```

```
{ flag=0, pos;
```

```
low=0, high=n-1;
```

```
for while (low <= high)
```

```
{
```

```
mid = (low+high)/2;
```

```
if ((a[mid] == key))
```

```
{ flag=1;
```

```
pos=mid+1;
```

```
break;
```

```
else if (key > a[mid])
```

```
low=mid+1;
```

```
else
```

```
high=mid-1;
```

```
if (flag==0)
```

```
printf("not found");
```

```
else printf("found at %d"; pos);
```

y

23/8/16

Hashing

UNIT - IV [4]

Hashin

Hash Table: This is a data structure which stores, has values associated with a hash key.

for example:

if we wanted to store 4 access employee records with attributes employee no., name, designation,

then we consider one of the field like as key field like employee no: for above record.

hash function takes this key as an i/p & produces an hash key which will be used as an index in to the hash table. to place the corresponding record of the given key at that location.

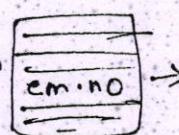
Same procedure is used to retrieve or search a record with a given key.

This process can locate a given record with one (or) few searches.

Hash tables are used to implement Dictionaries, consisting of key, value pair.

Em.no
no
key

\rightarrow HF(Key) \rightarrow Hash Key



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Ex 1 -

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key =

key =

key =

key =

Ex 2 : - L

key =

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Hashing Methods / Functions

- 1) Division Method
- 2) Mid Square Method
- 3) Multiplication Method
- 4) Folding Method.

Division Method:

In this method, we divide the key with the hash table size, which gives the address of the key.

Ex 1 :-

Let the H.T size = 10

$$\text{key} = 47$$

$$47 \div 10 = 4 \text{ remainder } 7$$

$$\text{key} = 32$$

$$32 \div 10 = 3 \text{ remainder } 2$$

$$\text{key} = 93$$

$$93 \div 10 = 9 \text{ remainder } 3$$

| hash Key | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----------|----|------|---|---|---|---|---|---|---|---|
| 0 | | | | | | | | | | |
| 1 | | | | | | | | | | |
| 2 | 32 | Name | | | | | | | | |
| 3 | 93 | Name | | | | | | | | |
| 4 | | | | | | | | | | |
| 5 | | | | | | | | | | |
| 6 | | | | | | | | | | |
| 7 | | | | | | | | | | |
| 8 | | | | | | | | | | |
| 9 | 47 | Name | | | | | | | | |

Ex 2 :- Let H.T Size = 100

$$\text{key} = 12475 \quad 12475 \div 100 = 75$$

Mid Square Method

We need square the key value, and then find the mid number of the squared value, which will be the address of the key.

Ex :- key = 3036

$$\text{HF(key)} = (3036)^2 = 91296$$

If H.T size is 10

then address is 7

| | | | | | | | | | |
|------|---|---|---|---|---|---|---|---|---|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 3036 | - | - | - | - | - | - | - | - | - |

Ex 2 :- 9217296

Fold

If HT size is 100
then address^{index} either 17 or 72

[for 7 we can

consider left no. or right number

but it should be same for all the values]

Ex 3 :-

9217296

If HT Size is 1000 (0-999)

Then 172 is the Hash key

Multiplication Method :-

Hash key = $H \cdot F(\text{key})$

$$= \text{floor}(A * (\text{key} * r))$$

where r is a real number.

PREFERRED VALUE FOR $r = 0.61803$

'A' can be any +ve int Ex:- 5, (but should be same for all the values)

Ex 1 :-

Key = 25

$$\text{Hash key} = \text{floor}(5 * (25 * 0.61803))$$

$$= \text{floor}(5 * 15.451)$$

$$= \text{floor}(77.255)$$

$$= 77$$

$$\begin{aligned} \text{floor}(3.7) \\ \text{floor}(3.1) \end{aligned}$$

$$\begin{aligned} \text{round}(3.7) = 4 \\ \text{round}(3.1) = 3 \end{aligned}$$

$$\begin{aligned} \text{Seal}(3.7) \\ \text{Seal}(3.1) \end{aligned}$$

Collis

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1) If s

2) If s

no c

3) The

key

4) If

collision

1) chain

2) line

3) queue

4) Do

Folding Method:

[fold & Sum]

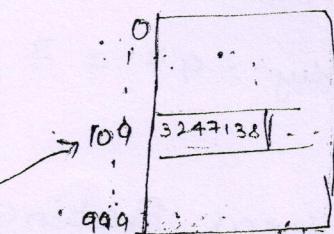
Key = 3247138

Let the HT Size is 1000 (0-999 indexes)

Hash key = 324 | 713 | 8

$$\begin{array}{r}
 324 \\
 713 \\
 + 8 \\
 \hline
 1045
 \end{array}$$

$104 + 5 = 109$



Collision:

If the hash function producing same hash key for two different key values then it is called collision.

Characteristic of a good hash function:-

- 1) It should be easy/simple to compute.
- 2) It should generate very few collisions; ideally no collisions at all.
- 3) The function should evenly distribute, hash keys, across the hash table.
- 4) It should operate on every bit of the i/p key.

Collision handling Methods:

- 1) Chaining.
- 2) Linear Probing
- 3) Quadratic Probing
- 4) Double hashing

Chaining :

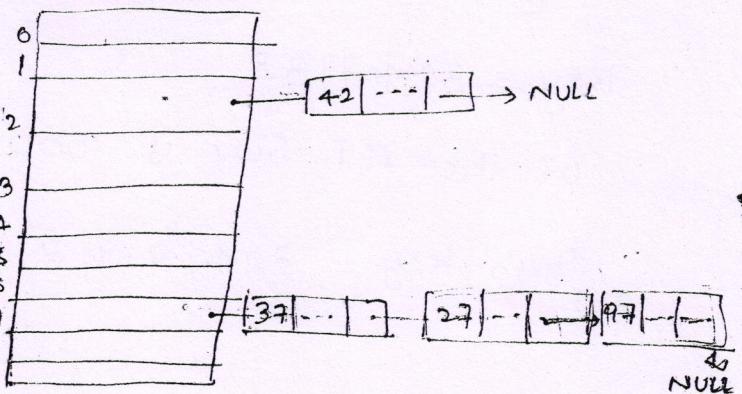
Method = Division Method

$$\text{Key} = 37 \equiv 7$$

$$\text{Key} = 42 \equiv 2$$

$$\text{Key} = 27 \equiv 7$$

$$\text{Key} = 97 \equiv 7$$



Linear Probing

Method = Division method.

$$\text{Key} = 37 \equiv 7$$

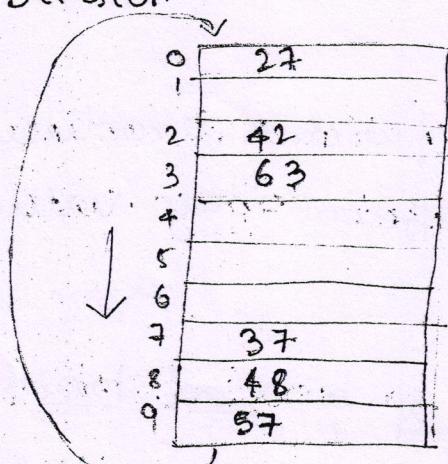
$$\text{Key} = 42 \equiv 2$$

$$\text{Key} = 48 \equiv 8$$

$$\text{Key} = 57 \equiv 7$$

$$\text{Key} = 63 \equiv 3$$

$$\text{Key} = 27 \equiv 7$$



Quadratic Probing

If collision occurs for given key

Then

$$\text{Hash Key} = (\text{Key} + x^2) \% \text{H.T Size}$$

where $x = 1, 2, 3, \dots$

Ex: i

key = 37 if collision occurs,

$$\text{Step 1: - Take } x=1 \text{ Hash Key} = (37+1^2) \% 10 = 38 \% 10 = 8$$

$$\text{Take } x=2 \text{ Hash Key} = (37+2^2) \% 10 = 41 \% 10 = 1$$

[If this index
is free use this
else go to
next 'x'
value]

$$\text{Take } x=3$$

Double Hashing :-

$$\text{HF1}(\text{key}) = \underline{\text{hash key}}$$

$$\text{HF2}(\text{key}) = \underline{M - \text{hash key}} = P$$

Now jump forward by P locations from collision index and place the record there

Key = 34

$$\text{HF}(34) = 34 \mod 10 = 4$$

Choose M as the biggest prime no less than size of the table

$$\text{if size} = 10$$

$$M = 7$$

$$\begin{aligned}\text{HF2}(34) &= |M - 4| \\ &= |7 - 4| \\ &= 3\end{aligned}$$

Collision index = 4

$$P = 3$$

jump to 7th index & place the record.

Rehashing :-

- The size of the hash table will be doubled to its nearest integer prime number, whenever, either the hash table becomes full (or overflow occurs) or the hash function producing more collisions.

17/9/16

Sorting Techniques

BUBBLE SORT

```
for (i=1 ; i<n ; i++)
```

```
{  
    for (j=0 ; j<n-1 ; j++)
```

```
        if (A[j] > A[j+1])
```

```
            temp = A[j]
```

```
            A[j] = A[j+1]
```

```
            A[j+1] = temp
```

```
}
```

```
}
```

```
}
```

Step 2:

Step 3:

Select

for

for

{

SELECTION SORT :-

Eg:-

| | | | | | | | | | |
|----|----|---|----|----|----|---|----|----|----|
| 10 | 13 | 7 | 53 | 62 | 69 | 4 | 46 | 35 | 12 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

Step 1: 10 13 7 53 62 69 4 46 35 12

7 13 10 53 62 69 4 46 35 12

7 13 10 53 62 69 4 46 35 12

7 13 10 53 62 69 4 46 35 12

7 13 10 53 62 69 4 46 35 12

4 13 10 53 62 69 7 46 35 12

4 13 10 53 62 69 7 46 35 12

4 13 10 53 62 69 7 46 35 12

4 13 10 53 62 69 7 46 35 12

Step 2:- * [4] 13 10 53 62 69 7 46 35 12

4 7 13 53 62 69 10 46 35 12

Step 3:- * [4] * [7] 13 53 62 69 10 46 35 12

Selection Sort

```
for (j=0 ; j < n-1 ; j++)
```

```
    for (k=j+1 ; k < n ; k++)
```

```
    { if [ A[j] > A[k] ]
```

```
        { tcmp = A[j] ;
```

```
            A[j] = A[k] ;
```

```
            A[k] = tcmp ;
```

```
        }
```

```
}
```

Double

? HFI (k)

HF2 (

NOW

6

Insertion Sort :

| | | | | | | |
|----|----|---|----|----|----|---|
| 10 | 13 | 7 | 53 | 62 | 69 | 4 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |

n = 7

while ($k \neq n$)

{ for ($i = k$; $i <= 0$; $i--$)

{ $j = i + 1$

if ($A[i] > A[j]$)

{

swap;

}

$i++$,

for ($i = 1$; $i < n$; $i++$)

{ $j = 1$;

while ($j > 0$ $\&$ $[j] < A[j - 1]$)

{ swap;

$j--$;

}

}

key = 3.

HF(34)

choo

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Reno

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the k

i occur
collis

Radix Sort :-

```
#include <stdio.h>
int get Max(int arr[], int n) {
    int mx = arr[0];
    int i;
    for(i=1; i<n; i++)
        if (arr[i]>mx)
            mx = arr[i];
    return mx;
}

void countsort(int arr[], int n, int exp)
{
    int output[n]; // Output array.
    int i, count[10] = {0};
    // Store count of occurrences in count[].
    for(i=0; i<n; i++)
        count[(arr[i]/exp)%10]++;
    for(i=1; i<10; i++)
        count[i] += count[i-1];
    count[i] = count[i] + count[i-1]
    // Build the output array.
    for(i=n-1; i>=0; i--)
    {
        output[count[(arr[i]/exp)%10]-1] = arr[i];
        count[(arr[i]/exp)%10]--;
    }
}
```

$a+b$
 $a=a+b$

$count[i] = count[i] + count[i-1]$

```

for (i=0; i<n; i++)
    arr[i] = output[i];
}

```

// The main function to that sorts arr[] of size n
using Radix Sort.

```

void radixSort(int arr[], int n) {
    int m = getMax(arr, n),
        exp;
    for (exp=1; m/exp>0, exp *= 10)
        countSort(arr, n, exp);
}

```

```

void print(int arr[], int n)
{
    int i;
    for (i=0; i<n; i++)
        printf("%d", arr[i]);
}

```

int main()

```

int arr[] = {170, 45, 75, 90, 802, 24, 2, 66},
    n = sizeof(arr)/sizeof(arr[0]),
    radixSort(arr, n),
    print(arr, n),
    return 0;
}

```

Step 1:

arr

[242
0]

out

[170]

Step 2

arr

[0 | 170 | 0]
[0 | 0 | 0]

count

O/P

[008 | 3 :
0]

output [count]

i = 8 out

i = 7 out

i = 6 out

i = 5 out

i = 4 out

i = 3 out

i = 2 out

i = 1 out

i = 0 out

Step 1:

| | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| arr | 042 | 170 | 323 | 894 | 666 | 047 | 449 | 170 | 008 |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

arr[] of size 9

| | | | | | | | | | |
|--------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Output | 170 | 042 | 323 | 894 | 666 | 047 | 008 | 170 | 449 |
|--------|-----|-----|-----|-----|-----|-----|-----|-----|-----|

| | | | | | | | | | |
|---------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| <u>Step 2</u> | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| arr | 170 | 042 | 323 | 894 | 666 | 047 | 008 | 179 | 449 |
| count | 0 | 1 | 1 | 2 | 3 | 4 | 5 | 6 | 8 |
| | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

| | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| O/P | 008 | 323 | 042 | 047 | 449 | 666 | 170 | 179 | 894 |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

$$\text{Output} \left[\text{Count} \left[\frac{\text{arr}[i] / \text{exp}}{\downarrow \text{last but 1 digit}} \cdot 10 \right] - 1 \right] = \text{arr}[i]$$

$$i=8 \quad \text{Output} \left[\text{Count}[4] - 1 \right] \Rightarrow O/P[5-1] = O/P[4] = \text{arr}[8]$$

$$i=7 \quad \text{Output} \left[\text{Count}[7] - 1 \right] \Rightarrow O/P[8-1] = O/P[7] = \text{arr}[7]$$

$$i=6 \quad \text{Output} \left[\text{Count}[0] - 1 \right] \Rightarrow O/P[1-1] = O/P[0] = \text{arr}[6]$$

$$i=5 \quad \text{Output} \left[\text{Count}[4] - 1 \right] \Rightarrow O/P[4-1] = O/P[3] = \text{arr}[5]$$

$$i=4 \quad \text{Output} \left[\text{Count}[6] - 1 \right] \Rightarrow O/P[6-1] = O/P[5] = \text{arr}[4]$$

$$i=3 \quad \text{Output} \left[\text{Count}[9] - 1 \right] \Rightarrow O/P[9-1] = O/P[8] = \text{arr}[3]$$

$$i=2 \quad \text{Output} \left[\text{Count}[2] - 1 \right] \Rightarrow O/P[2-1] = O/P[1] = \text{arr}[2]$$

$$i=1 \quad \text{Output} \left[\text{Count}[4] - 1 \right] \Rightarrow O/P[3-1] = O/P[2] = \text{arr}[1]$$

$$i=0 \quad \text{Output} \left[\text{Count}[7] - 1 \right] \Rightarrow O/P[7-1] = O/P[6] = \text{arr}[0]$$

| Step 3: | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| arr. | 008 | 323 | 042 | 047 | 449 | 666 | 170 | 179 | 894 |

Radix Sort

| Count: | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|--------|---|---|---|---|---|---|---|---|---|---|
| | 3 | 2 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 |

| O/P | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|-----|---|---|---|---|---|---|---|---|---|
| | | | | | | | | | |

$$\text{output} = \left[\text{count}[(\text{arr}[i] / (\text{exp})) \% 10] - 1 \right] = \text{arr}[i]$$

$$i=8 \quad \text{output} [\text{count}[8] - 1] \Rightarrow \text{OP} [$$

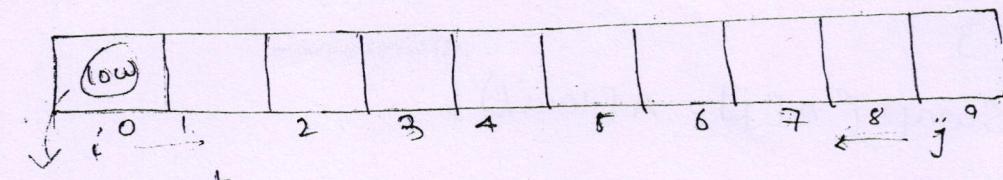
```
#include
int get
int mx
int i;
for(i=1;
if (a
mx
return
}
```

```
void col
{
int Out
int i,
// Sto
for (i
com
for (i
co
// Buil
for (i
{
out
cou
}
```

```
// Buil
for (i
{
out
cou
}
```

27/9/16

Quick Sort:-



$$\text{Pivot} = A[\text{low}]$$

Increment i such that it should be greater than the Pivot element

$$A[i] \leq \text{Pivot}$$

Move j towards left ^(decreased), such that the value should be less than the Pivot element $A[j] > \text{Pivot}$.

After the increment of i & j values.

If $i < j$ (index values)

Swap the elements

If $j < i$ then Swap $A[j]$ with Pivot value or $A[\text{low}]$

#include <stdio.h>

int Partition (int A[10], int low, int high)

{

 int Pivot = A[low], i, j;

 i = low;

 j = high;

 while ($i \leq j$)

 {

 while ($A[i] \leq \text{Pivot}$)

$i++$;

 while ($A[j] > \text{Pivot}$)

$j--$;

⑧
this index
cc use this
go to
next x'
value

29/9

```
if (i < j)
    swap (A[i], A[j]);
}
swap (A[j], A[low]);
return j;
}
void quicksort (int A[], int low, int high)
{
    int k;
    if (low < high)
    {
        k = partition (A, low, high);
        quicksort (A, low, k-1);
        quicksort (A, k+1, high);
    }
}
```

void swap (

{

}

void main ()

{

int A[10];

for (i=0; i < j; i++)
 pf

sf

read A;

display A;

quicksort (A, 0, 9);

display A;

}

Void

{

int

for

{

int

PC

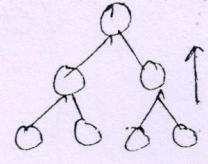
W

{

18/10

29/9/16

Heap Sort:



void makeheap [int A[10], int n)

{

 int i, val, j, Parent;

 for(i=1; i<n; i++)

 { val = arr[i];

 j = i;

 Parent = (j-1)/2;

 while(j>0 && A[Parent] < val)

 {

 A[j] = A[Parent];

 j = Parent;

 Parent = (j-1)/2..

 }

 A[j] = val;

 }

3

| | | | | | | | | | | | |
|---|---|----|----|----|----|----|----|----|----|----|----|
| 8 | 7 | 10 | 26 | 16 | 45 | 89 | 43 | 69 | 39 | 54 | 17 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |

Void heap sort [int A[10], int n)

{

int i, k, temp, j;

for (i=n-1; i>0; i--)

{

temp = A[i];

A[i] = A[0];

k=0; K = Parent index
j = child index

if (i==1)

j = -1;

else j = 1;

if (i>2 && A[2]>A[1])

j = 2;

while (j>=0 && temp < A[j])

{

A[k] = A[j];

k=j;

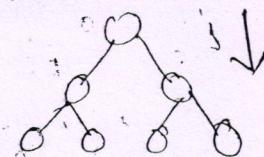
j = 2 * k + 1; (going to left child)

if (j+1 <= i-1 && A[j] < A[j+1])

j++;

if (j > i-1)

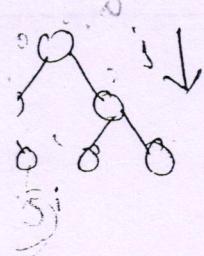
j = -1;



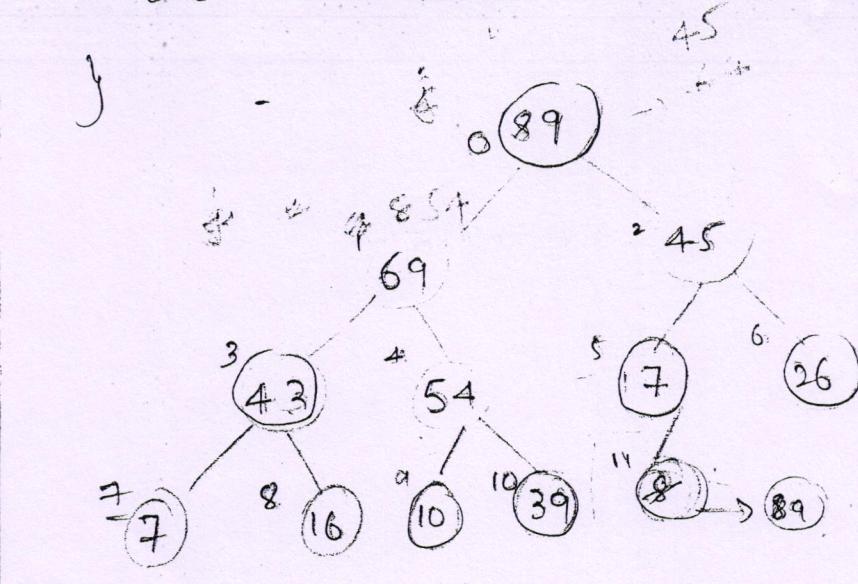
here i = no. of elements
delte
(and)
also for no. of
elements it should
consider for each
iteration.

Step
i
tu

$A[k] = \text{temp}$;



elements to
insert
and
or no. of
it should
for each



Step 1:
 $i = 11$; $11 > 0$

$\text{temp} = A[i] = 8$; $k = 0$

$A[i] = 89$; $j = 1$

$i > 2$

$45 > 69 \times$

$i > 0$
 $A[0] = A[1]$
 $A[0] = 69$

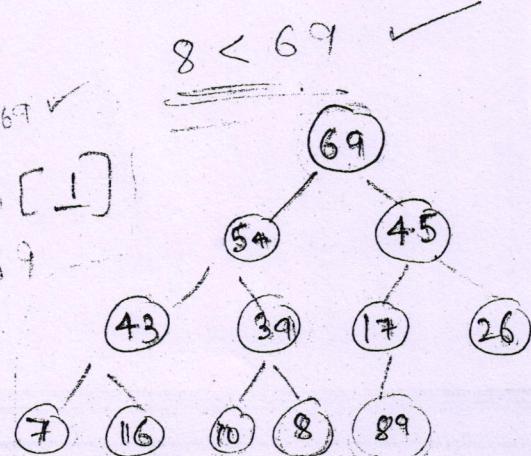
$k = 1$

$j = (2 * 1) + 1$

~~$= 3$~~

$k = 3$

~~$= 10$~~



After Step 1

$A[3] < A[4]$

~~$54 < 43 \times$~~

$43 < 54 \checkmark$

$k = 1$ $j = 4$ $A > 11 - 1$

$A[3] < A[4]$

